

Arthur E. Imperatore School of Sciences and Arts

Department of Mathematical Sciences

Seminar

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On the characterization of the source-to-all-terminal diameter-constrained reliability domination

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Abstract: Let G = (V, E) be a digraph with a distinguished set of terminal vertices $K \subseteq V$ and a vertex $s \in K$. We define the s, K-diameter of G as the maximum distance between s and any of vertices of K. If the arcs fail randomly and independently with known probabilities (vertices are always operational), the Diameter-constrained s, K-terminal reliability of G, $R_{s,K}(G, D)$, is defined as the probability that surviving arcs span a subgraph whose s, K-diameter does not exceed D.

A graph invariant called the domination of a graph G was introduced by Satyanarayana and Prabhakar to generate the non-canceling terms of the classical reliability expression, $R_{s,K}(G)$, based on the same reliability model (i.e. arcs fail randomly and independently and where nodes are perfect), and defined as the probability that the surviving arcs span a subgraph of G with unconstrained finite s, K-diameter. This result allowed the generation of rapid algorithms for the computation of $R_{s,K}(G)$.

In this paper we present a characterization of the diameter-constrained s, K-terminal reliability domination of a digraph G = (V, E) with terminal set K = V, and for any diameter bound D, and, as a result, we solve the classical reliability domination, as a specific case. Moreover we also present a rapid algorithm for the evaluation of $R_{s,V}(G, D)$.